

A matrix A is called symmetric if $A^T = A$

Example $A = \begin{pmatrix} 1 & 2 \\ 2 & 3 \end{pmatrix}$, $B = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}$

A is symmetric since $A^T = A$

B is not symmetric since $B^T \neq B$

Properties of symmetric matrix

1) If A is symmetric then A^T is symmetric

2) If A and B are symmetric then $A+B$ is symmetric

3) If A and B are symmetric then AB is symmetric iff $AB = BA$

A matrix A is called anti symmetric if $A^T = -A$

Example $A = \begin{pmatrix} 1 & 2 \\ -2 & -1 \end{pmatrix}$ is anti symmetric since $A^T = -A$

Properties of anti symmetric matrix

1) If A is anti symmetric then A^T is anti symmetric

2) If A and B are anti symmetric then $A+B$ is anti symmetric

3) If A and B are anti symmetric then AB is anti symmetric iff $AB = -BA$

The inverse of matrix

An $n \times n$ matrix is called nonsingular (invertible) if there is $n \times n$ matrix B such that AB

$$= BA =$$

The matrix B is called an inverse of A (denoted by)

If there exists no matrix B then A is called singular (noninvertible)

Example Let $A =$, $B =$, $AB = BA =$

B is an inverse of A (A is non singular)

If a matrix has an inverse then the inverse is unique

Properties of inverse

1) If A is non singular then A^{-1} is non singular and $(A^{-1})^{-1} = A$

2) If A and B are non singular then AB non singular and $(AB)^{-1} = B^{-1}A^{-1}$

3) If A is non singular then $(A^{-1})^{-1} = A$

Example Find the inverse of $A =$

$$=$$

$$=$$

$$= 1 \quad , \quad = 0$$

$$= 0, = 1$$

$$A = -2, b = 1, c = 3/2, d = -1/2$$

=

Gauss Jordan method

Example A =

[A:] =

Divided first row on 3

Multiply first row by -2 and add to second row. Multiply first row by -4 and add to
third row